

**UNIT 6 LESSONS 1-2**

**PRECALCULUS A**



**LESSONS:**

- Analytic Geometry
- Introduction to Conic Sections

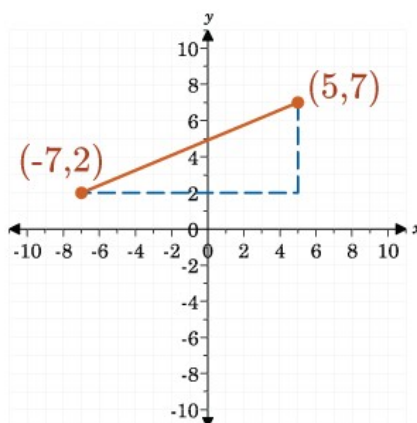
## ANALYTIC GEOMETRY

- the study of geometric figures using the coordinate plane
- and using algebraic equations to represent geometric shapes

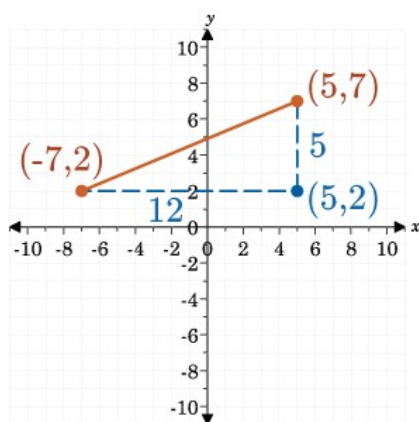
“analyzing shapes on a graph with algebra”



Let's start with analyzing the length of simple line segments.

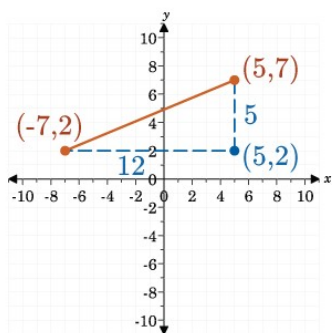


To get from one endpoint to the next, it shifts both horizontally and vertically. We can count how far for each shift.



You know what comes next for finding the length of the first segment . . .

The Pythagorean Theorem!



$$a^2 + b^2 = c^2$$

$$12^2 + 5^2 = c^2$$

$$144 + 25 = c^2$$

$$169 = c^2$$

$$13 = c$$

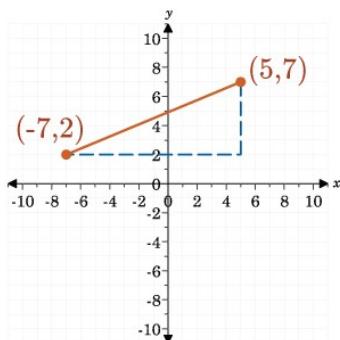
So, yes, this is taking us to the  
**Distance Formula!**

$$\begin{array}{l}
 a^2 + b^2 = c^2 \\
 12^2 + 5^2 = c^2 \\
 144 + 25 = c^2 \\
 169 = c^2 \\
 13 = c
 \end{array}
 \qquad
 \begin{array}{l}
 a^2 + b^2 = c^2 \\
 (x_2 - x_1)^2 + (y_2 - y_1)^2 = c^2 \\
 \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = c
 \end{array}$$



Next analysis is the Midpoint!

$$M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$



$(-1, 9/2)$



Your turn . . .

$(-5, 3)$  and  $(3, -5)$

Distance = ?

Midpoint = (?, ?)



Your turn . . .

$(-5, 3)$  and  $(3, -5)$

Distance =  $8\sqrt{2}$

Midpoint =  $(-1, -1)$



Do you remember how  
to simplify a radical??

Do a factor tree, and look for  
perfect squares.

$$\sqrt{25}$$

$$\sqrt{125}$$

$$\sqrt{60}$$



Do you remember how  
to simplify a radical??

Do a factor tree, and look for  
perfect squares.

$$\sqrt{25}$$

$$\sqrt{125}$$

$$\sqrt{60}$$

$$\sqrt{5 \cdot 5}$$

$$\sqrt{5 \cdot 5 \cdot 5}$$

$$\sqrt{2 \cdot 2 \cdot 3 \cdot 5}$$



Do you remember how  
to simplify a radical??

Do a factor tree, and look for  
perfect squares.

$$\sqrt{25}$$

$$\sqrt{5*5}$$

$$5$$

$$\sqrt{125}$$

$$\sqrt{5*5*5}$$

$$5\sqrt{5}$$

$$\sqrt{60}$$

$$\sqrt{2*2*3*5}$$

$$2\sqrt{15}$$



Remember,  
don't give a decimal answer unless  
the question asks for it.

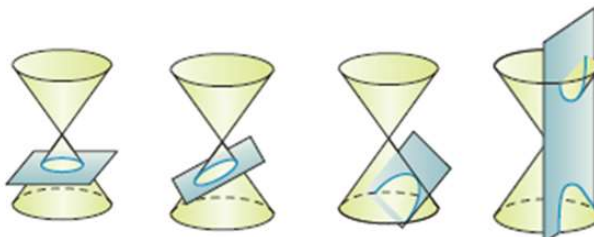


An improper fraction or  
a simplified radical  
is the exact amount.

Rounding off a decimal is an  
approximate answer.



## CONIC SECTIONS



CIRCLE

ELLIPSE

PARABOLA

HYPERBOLA

... the intersections of a plane and a double right circular cone.

## CONIC SECTIONS

### General Equation of a Conic Section

The equation of every conic section can be written in the following form:

$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$ , where  $A$ ,  $B$ ,  $C$ ,  $D$ ,  $E$ , and  $F$  are real numbers.

... This format covers all four conic section types.

... But how to tell which type from this format?



## CONIC SECTIONS

### General Equation of a Conic Section

The equation of every conic section can be written in the following form:

$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$ , where  $A, B, C, D, E,$  and  $F$  are real numbers.

### Identifying a Conic Section from Its General Equation

The discriminant of the equation is  $B^2 - 4AC$ .

- If  $B^2 - 4AC > 0$ , the conic is a hyperbola.
- If  $B^2 - 4AC = 0$ , the conic is a parabola.
- If  $B^2 - 4AC < 0$  and  $A = C$ , the conic is a circle.
- If  $B^2 - 4AC < 0$  and  $A \neq C$ , the conic is an ellipse.

### IDENTIFYING CONIC SECTIONS FROM GENERAL FORM

- ✓ First, multiply/distribute/rearrange to get the equation into the general form.
- ✓ Then, identify the numbers in the  $A, B,$  &  $C$  positions. (Sometimes they can be zero.)
- ✓ Calculate the Discriminant, and check the guidelines for which shape it is.

$$y^2 - 8x - 10y + 1 = 0$$

$$(x+4)^2 + (y-2)^2 = 3$$

**IDENTIFYING CONIC SECTIONS  
FROM GENERAL FORM**

$$y^2 - 8x - 10y + 1 = 0$$

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

**IDENTIFYING CONIC SECTIONS  
FROM GENERAL FORM**

$$y^2 - 8x - 10y + 1 = 0$$

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

$$A = 0, B = 0, \text{ and } C = 1$$

$$B^2 - 4AC$$

$$0^2 - 4(0)(1) = 0$$

**IDENTIFYING CONIC SECTIONS  
FROM GENERAL FORM**

$$y^2 - 8x - 10y + 1 = 0$$

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

$$A = 0, B = 0, \text{ and } C = 1$$

$$B^2 - 4AC$$

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**PARABOLA**

**IDENTIFYING CONIC SECTIONS  
FROM GENERAL FORM**

$$(x+4)^2 + (y-2)^2 = 3$$

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

**IDENTIFYING CONIC SECTIONS  
FROM GENERAL FORM**

$$(x+4)^2 + (y-2)^2 = 3$$

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

$$(x^2 + 8x + 16) + (y^2 - 4y + 4) = 3$$

$$x^2 + y^2 + 8x - 4y + 17 = 0$$

**IDENTIFYING CONIC SECTIONS  
FROM GENERAL FORM**

$$(x+4)^2 + (y-2)^2 = 3$$

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

$$(x^2 + 8x + 16) + (y^2 - 4y + 4) = 3$$

$$x^2 + y^2 + 8x - 4y + 17 = 0$$

$$A = 1, B = 0, \text{ and } C = 1$$

$$B^2 - 4AC$$

$$0^2 - 4(1)(1) = -4$$

### IDENTIFYING CONIC SECTIONS FROM GENERAL FORM

$$(x+4)^2 + (y-2)^2 = 3$$

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

$$(x^2 + 8x + 16) + (y^2 - 4y + 4) = 3$$

$$x^2 + y^2 + 8x - 4y + 17 = 0$$

$$A = 1, B = 0, \text{ and } C = 1$$

$$B^2 - 4AC$$

$$0^2 - 4(1)(1) = -4$$

**CIRCLE**

### THAT'S IT FOR NOW ON CONIC SECTIONS!



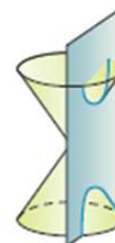
CIRCLE



ELLIPSE



PARABOLA



HYPERBOLA

**More Details Coming in the next lessons!**

## Questions??

Review the [Key Terms](#) and [Key Concepts](#) documents for this unit.

Look up the topic at [khanacademy.org](http://khanacademy.org) and [virtualnerd.com](http://virtualnerd.com)

Check our class website at [nca-patterson.weebly.com](http://nca-patterson.weebly.com)

\*Reserve a time for a call with me at  
[jpattersonmath.youcanbook.me](http://jpattersonmath.youcanbook.me)  
We can use the LiveLesson whiteboard  
to go over problems together.

